

Additional file 1. Estimating molecular size and surface density

The molecular surface density calculation for the QCM biosensor's quartz crystal reaction surface was based on estimating the globular molecular radius (R) of the 40.1kDa DBL5ε domain fragment [1] and using the Sauerbrey equation for the relationship between change in quartz resonance frequency and change in mass [2]. The equation was modified to consider a reaction in water rather than the original assumption of a reaction in air [3]. This gave,

$$R = \left(\frac{3 \cdot M_w \cdot \nu}{4 \cdot \pi \cdot N_A} \right)^{\frac{1}{3}} \quad \text{(Equation I)}$$

Where ν is the partial specific volume of the molecule of interest, (volume per mass, taken to be 0.7317 ml x g⁻¹, a molecular constant calculated based on the composition of an average protein), and N_A is Avogadro's Constant (6.022 x 10²³ mol⁻¹).

For the FCR3-derived VAR2CSA DBL5ε domain fragment, this gave a molecular radius of

$$R = \left(\frac{3 \cdot 40100 \text{Da} \cdot 0.7317 \frac{\text{ml}}{\text{g}}}{4 \cdot 3.1415 \cdot 6.022 \cdot 10^{23} \text{mol}^{-1}} \right)^{\frac{1}{3}} \approx 2.27 \cdot 10^{-7} \text{cm} = 2.27 \text{nm}$$

Change in mass is a linear function of the change in frequency [2]. Equation II then describes the change in mass on the surface of a crystal with one liquid-exposed surface.

$$\Delta m = \frac{\Delta f \cdot A \sqrt{\rho_q \mu_q}}{-2 \left(f_0 - f_0^{\frac{3}{2}} \sqrt{\frac{\eta_l \rho_l}{\pi \mu_q \rho_q}} \right)^2} \quad \text{(Equation II)}$$

Where f_0 is the resonant frequency of the quartz crystal measured in Hz (10MHz), A is the piezo-electrically active crystal area (0.25cm^2), ρ_q is the density of quartz (2.648g/cm^3), μ_q is the shear modulus of quartz for an AT-cut crystal ($2.947 \times 10^{11}\text{g/(cm}\cdot\text{s}^2)$), η_l is the dynamic viscosity of the liquid ($6.91 \times 10^{-3}\text{g/(cm}\cdot\text{s)}$ for water at 37°C), and ρ_l is the density of the liquid (0.993g/cm^3 for water at 37°C). Δm is calculated in grams.

Reference List

1. Rodbard D, Chrambach A: **Estimation of molecular radius, free mobility, and valence using polyacrylamide gel electrophoresis.** *Anal Biochem* 1971, **40**:95-134.
2. Sauerbrey G: **Verwendung von Schwingquarzen zur Wägung dünner Schichten und zur Mikrowägung.** *Z Phys* 1959, **155**:206-215.
3. Kanazawa KK, Gordon JG: **Frequency of a quartz microbalance in contact with liquid.** *Anal Chem* 1985, **57**:1770-1771.